

1) a) $P(y_{i2}=1 | y_{i1}=0, x_{i1}, x_{i2}, \alpha_c) = P(y_{i2}=1 | x_{i1}, x_{i2}, \alpha_c) = \Lambda(\alpha_c + x_{i2}'\beta_0)$

b) $1 - \Lambda(\alpha_c + x_{i2}'\beta_0)$

c) note
$$P(y_{i2}=1 | y_{i1} \neq y_{i2}, x_{i1}, x_{i2}, \alpha_c) = \frac{P(y_{i2}=1, y_{i1} \neq y_{i2} | x_{i1}, x_{i2}, \alpha_c)}{P(y_{i1} \neq y_{i2} | x_{i1}, x_{i2}, \alpha_c)}$$

$$= \frac{P(y_{i2}=1, y_{i1}=0 | x_{i1}, x_{i2}, \alpha_c)}{P(y_{i2}=1, y_{i1}=0 | x_{i1}, x_{i2}, \alpha_c) + P(y_{i2}=0, y_{i1}=1 | x_{i1}, x_{i2}, \alpha_c)}$$

$$= \frac{1}{1 + e^{-\alpha_c - x_{i1}'\beta_0}} \frac{e^{-\alpha_c - x_{i2}'\beta_0}}{1 + e^{-\alpha_c - x_{i1}'\beta_0}}$$

$$\frac{1}{1 + e^{-\alpha_c - x_{i1}'\beta_0}} \frac{e^{-\alpha_c - x_{i1}'\beta_0}}{1 + e^{-\alpha_c - x_{i1}'\beta_0}} + \frac{1}{1 + e^{-\alpha_c - x_{i1}'\beta_0}} \frac{e^{-\alpha_c - x_{i2}'\beta_0}}{1 + e^{-\alpha_c - x_{i2}'\beta_0}}$$

$$= \frac{e^{-\alpha_c - x_{i1}'\beta_0}}{e^{-\alpha_c - x_{i1}'\beta_0} + e^{-\alpha_c - x_{i2}'\beta_0}} = \frac{e^{-x_{i1}'\beta_0}}{e^{-x_{i1}'\beta_0} + e^{-x_{i2}'\beta_0}}$$

does not depend on α_c

similarly can get $P(y_{i1}=1 | y_{i1} \neq y_{i2}, x_{i1}, x_{i2}, \alpha_c)$
 So we have probability function for each i , conditional on $y_{i1} \neq y_{i2}$, and can do MLE for those who "switch" over time.

$$3) \frac{1}{n} \leq d_c \log \frac{1}{\sigma} \phi\left(\frac{x-x_0}{\sigma}\right) + (1-d_c) \Phi\left(\frac{y_c-x_0}{\sigma}\right)$$

same in both cases, a) and b)